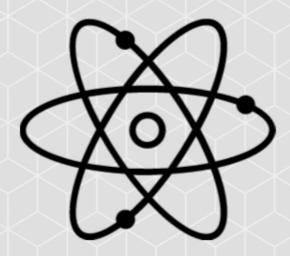
Open-Access

PHYSICS FOR THE LIFE SCIENCES

Solution Manual



Created by WebStraw



Physics for the Life Sciences – Electricity Solutions

Introduction:

Dear student,

Thank you for opening this solution manual for the Electricity chapter of the Physics for the Life Sciences Question Manual. This resource has been created by members of the Education Team at WebStraw who have previously taken an introductory university physics course.

Purpose:

This resource is meant to supplement the Physics for the Life Sciences Question Manual, by providing solutions to select questions. To access the full question manual, please click here.

Instructions

We recommend first trying to complete the problems in the question manual on your own. If you get stuck, you can use this resource to view the solution provided by one of our Education Team members. Once you are confident you understand how to solve that question, we recommend solving additional related problems in order to successfully master the topic.

Disclaimer

This resource assumes that you have a basic understanding of key concepts related to the Electricity unit in physics. If you are looking to improve your understanding of specific physics content, check out the additional resources provided at the end of the question manual.

<u>Note:</u> There may be more than one correct method to solve some of the problems outlined in the question manual. Thus, the solutions provided may not represent the only acceptable solution.

If you have any comments or feedback regarding this resource or the solutions contained in it, please do not hesitate to contact us at team@webstraw.ca

We wish you the best of luck on your learning journey!

- The WebStraw Education Team

The equation for force between 2 charges is $F = \frac{k9.192}{r^2}$. (f you double the distance (r \rightarrow 2r) and halve the charges $(q_1 \rightarrow \frac{1}{2}q_1$ you double the airrance (r - 2 - 2), and $q_2 \rightarrow \frac{1}{2}q_2$, we get $F_2 = \frac{k(\frac{1}{2}q_1)(\frac{1}{2}q_2)}{(2r)^2} = \frac{\frac{1}{4}kq_1q_2}{4r^2} = \frac{1}{16}\left(\frac{kq_1q_2}{r^2}\right)$

G3:

Given:
$$m = 10 \text{ kg}$$
 $E = 2 \frac{N}{C}$ $\alpha = 20 \frac{m}{S^2}$

Required: Charge (q) on object

Solve:
$$F = q E$$
 but $F = ma$ so $qE = ma$
 $q = \frac{ma}{E} = \frac{(lokg)(20\frac{m}{52})}{(2\frac{N}{C})} = \frac{100 C}{100 C}$

<u>65.</u>

Given:
$$r = 10mm = 0.01m$$
 $q = 4.10^{-9}$

Required: Electric field

Solve:
$$E = \frac{kq}{r^2} = (8.99 - 10^9)(4.10^{-9}) = 359600 \frac{N}{C}$$

67:

Given:
$$E = 1.14 \cdot 10^6 \frac{N}{c}$$
 $V_f = 5.3 \cdot 10^5 \frac{m}{s}$ $V_7 = 0 \frac{m}{s}$ $q = 1.6 \cdot 10^{-19} C$
 $m = 1.67 \cdot 10^{-27} \text{ kg}$

Required: time to reach final relocity

Solve:
$$F = q E = (1.6 \cdot 10^{-17} C)(1.14 \cdot 10^6 \frac{N}{C}) = 1.824 \cdot 10^{-13} N$$

$$F = ma \Rightarrow a = \frac{F}{m} = \frac{1.824 \cdot 10^{-13} N}{1.67 \cdot 10^{-27} kg} = 1.69 \cdot 10^{14} \frac{m}{s^2}$$

$$V_{+}^{2} = V_{+} + at \Rightarrow t = \frac{V_{+} - V_{0}}{a} = \frac{(5.3 \cdot 10^{5} \frac{m}{s} - 0\frac{m}{s})}{(1.09 \cdot 10^{14} \frac{m}{s^2})} = \frac{1.8 \cdot 10^{-9} S}{a}$$

An electron (negative charge) will move in the direction opposite to the field lines, it experience a force of F=qE=eE where e 15 the elementary charge, A proton will experience the same force, but more in the direction of the field lines as it is Positively charged.

Given: $E = 100 \frac{N}{c}$ q = Q m = M

Required in in terms of Q & E

Solve: Object experiences electric force upwards & gravitational force (weight) downwards

Fe = qE = QE > when it floats, Fret = 0 so Fe = Fg $F_q = F_e \longrightarrow mg = QE$ so $m = \frac{QE}{g} = \sqrt{\frac{QE}{q.8}}$ Fg= mg

Given: E = 25000 (parallel plate capacitor generates a field between its plates)

q=e=1.6-10-19 (m=1.67.10-27 kg d= 10 mm = 0.01m

Required: Speed of electron at positive plate

Solve: F=qE=ma -> a=qE=2,395-1012 ==

Vf2 = Vo2 + 2ad -> Vf = \(Vo2 + 2ad = \[2.19 - 10^5 \]

Solve:
$$P = V^2/R$$
 $\Rightarrow V = \sqrt{PR} = 122V$

$$P = IV \Rightarrow I = \frac{P}{V} = 6.12A$$

917:

Given:
$$q = 1.6 \cdot 10^{-19} \text{ C}$$
 $V_f = 24.4 \cdot 10^5 \frac{\text{m}}{\text{s}}$ $m = 80.4 \cdot 10^5 \frac{\text{m}}{\text{s}}$

Required: Voltage

Solve: All of electric energy is converted into kinetic energy

$$E_e = qV$$
 $E_k = \frac{1}{2}mv^2$

$$V = \frac{1}{2} \frac{mv^2}{q} = 31070 \text{ V}$$

Required: Work done

Given:
$$E = 5000 \frac{V}{m}$$
 travelling to right $d = 2 m$ $q = 1.6 \cdot 10^{-19} C$
 $m = 1.67 \cdot 10^{-27} \text{ kg}$

Required:
$$V_f$$
 at left plate
Solve: $F = qE = ma$ $\longrightarrow a = \frac{qE}{m} = 4.79 - 10'' \frac{m}{s^2}$

$$= \sqrt{V_0^2 + 2ad}$$

$$= \sqrt{1.38 \cdot 10^6 \text{ m/s}}$$

Griven: $q = 1.6 \cdot 10^{-19} \text{ C}$ m = $1.67 \cdot 10^{-27}$ kg V = 100V $V_i = 100 \cdot 000 \frac{m}{5}$ Required: VI

Solve: Fk + Ee = Ek + E/f and all of the Ee is converted to Ek Ek + E = Ek $\frac{5}{1} m v_1^2 + 9 \Lambda = \frac{5}{1} m v_2^2 \longrightarrow 8.35 \cdot 10^{-18} 2 + 1.6 \cdot 10^{-17} 2 = \frac{5}{12} m v_2^2$

$$V_{4} = \sqrt{\frac{170768 \frac{m}{5}}{170768 \frac{m}{5}}}$$

The charge is moving towards A (moving with the field lines) So it must be a positive charge (magnitude cannot be found)

If charge is doubled, it will move in the same direction, but experience a larger force (F=qE) so will have greater acceleration & more faster along the path

G251.

If charge is reversed, it will move in the opposite direction (towards B).

$$= C_1 + C_2 = 2C$$

$$C_{eq} = C_1 + C_2 = 2C \qquad C_{eq} = \left(\frac{1}{C} + \frac{1}{C}\right)^{-1} = \frac{1}{2}C \qquad C_{eq} \quad halves.$$

Full voltage drop across each capacitor

across each capacitor.
$$U = \frac{1}{2} CV^2$$

Each capacitor has half their original voltage drop.

$$V = \frac{1}{2} \left(\left(\frac{v}{2} \right)^2 = \frac{1}{4} \left(\frac{1}{2} CV^2 \right)$$

V at each capacitor decreases by a factor

Q doubles

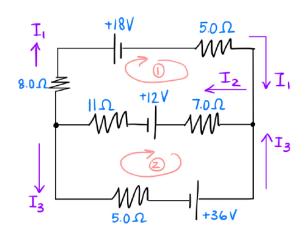
629.

Given: V=550V d=3.6mm = 0.0036m initial position = 2.1mm from + plate

Required: work to more it 0.0036 m to - plate

Solve: The energy gained = the work performed by the field |W|= |q DV| = (1.6.10-19)(100,000) = [1.6.10-14]

G33.



* selected random directions of current and random directions of travel to start.

Node Law:

$$I_1 + I_3 - I_2 = 0$$

Loop Law:

Node Law + substitution

$$I_{1} + I_{3} = I_{2}$$

$$-\left(\frac{30 + 18I_{2}}{13}\right) + \frac{24 - 18I_{2}}{5} = I_{2}$$

$$\frac{-5(30 + 18I_{2}) + 13(24 - 18I_{2})}{65} = I_{2}$$

$$-150 - 90I_{2} + 3I_{2} - 234I_{2} = 65I_{2}$$

$$162 = 389I_{2}$$

$$I_{2} = 0.42A$$

$$I_{1} = -\left(\frac{30 + 18I_{2}}{13}\right)$$

$$I_{1} = -2.9$$

$$I_{3} = \frac{24 - 18I_{2}}{5}$$

$$I_{3} = 3.3A$$

The current through the $8.0\,\Omega$ and the top $5.0\,\Omega$ resistors is $2.9\,A$. The current through the $II\Omega$ and $7.0\,\Omega$ resistors is $0.42\,A$. The current through the bottom $5.0\,\Omega$ resistor is $3.3\,A$.

No solution available for G35

Required: time constant 7

Solve: Resistors in series so
$$R_t = R_1 + R_2 = 1200 \Omega$$

 $T = R_t C = (50.10^{-6} F)(1200 \Omega) = [0.06]$

If in parallel,
$$R_{+} = \left(\frac{1}{\frac{1}{R_{1}} + \frac{1}{R_{2}}}\right) = 266.67 \Omega$$

 $T = R_{+}C = (50.10^{-6} \text{ F})(266.67 \Omega) = [0.013]$

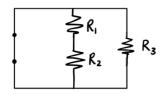
. T decreases if resistors arranged in parallel

G39.

Possible circuit diagram:

$$R_1 = 2.0 \Omega$$

 $R_2 = 3.0 \Omega$
 $R_3 = 4.0 \Omega$



①
$$R_{12} = R_1 + R_2 = 2.0 \Omega + 3.0 \Omega = 5.0 \Omega$$

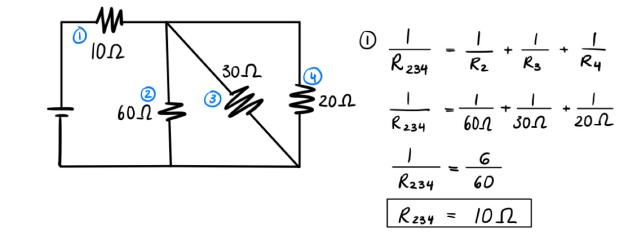
$$\frac{1}{R_{123}} = \frac{1}{R_{12}} + \frac{1}{R_{3}}$$

$$\frac{1}{R_{123}} = \frac{1}{5.00} + \frac{1}{4.00}$$

$$\frac{1}{R_{123}} = \frac{9}{20}$$

.. The equivalent resistance in this circuit is 2.2 Ω .





Therefore, the equivalent resistance in the circuit is 2012.

The voltage across each resistor is 21 V.

a)
$$P = \frac{V^2}{R} = \frac{(21V)^2}{5\Omega} = 88 \text{ W}$$

: 88 W of power is expended at the $5.0-\Omega$ resistor.

b)
$$P = \frac{V^2}{R}$$

$$R = \frac{V^2}{P} = \frac{(2|V|)^2}{30W} = 15 \Omega$$

.. The resistance of the second resistor is 15Ω .

G45.
$$I = 1.0 A$$

$$V = 800 V$$

$$\rho = IV = \frac{\Delta E}{\Delta t}$$

$$(1.0A)(800V) = \frac{0.88 J}{\Delta t}$$

$$\Delta t = 0.0011 s$$

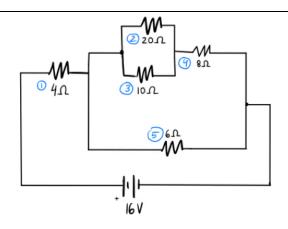
The shock is delivered over 0.00115 (1.1 ms).

G47. a)
$$\frac{1}{R_{23}} = \frac{1}{R_2} + \frac{1}{R_3}$$

$$\frac{1}{R_{23}} = \frac{1}{20\Omega} + \frac{1}{10\Omega}$$

$$\frac{1}{R_{23}} = \frac{3}{20\Omega}$$

$$R_{23} = 6.67\Omega$$



Therefore, the combined resistance of the 20- Ω and 10- Ω resistors is 6.67 Ω .

b)
$$R_{234} = R_{23} + R_4$$

= 6.67\Omega + 8\Omega = 14.67\Omega

= 14.67 \(\Omega \) Therefore, R 234 is 14.67 \(\Omega \).

$$\frac{1}{R_{2345}} = \frac{1}{R_{234}} + \frac{1}{R_{5}}$$

$$\frac{1}{R_{2345}} = \frac{1}{14.67\Omega} + \frac{1}{6\Omega}$$

 $R_{2345} = 4.26 \Omega$ Therefore, $R_{2345} = 4.26 \Omega$

A)
$$R_{12345} = R_1 + R_{2345}$$

 $R_{12345} = 4\Omega + 4.26\Omega$
 $Req = 8.3\Omega$

Therefore, Req is 8.3.1.

e)
$$I = \frac{V}{R} = \frac{16 \, V}{8.26 \, \Omega} = \boxed{1.9 \, A}$$

Therefore, the total current in the circuit is 1.9 A.

$$T_{5} + T_{234} = T_{total} = 1.9A$$

$$\frac{5}{2} T_{234} + T_{234} = 1.9A$$

$$\frac{7}{2} T_{234} = 1.9A$$

$$I_{234} = 0.543 A$$

f) $R_5 = 0.409 R_{234} \approx \frac{2}{5} R_{234}$:: R_5 will have $\frac{5}{2}$ times more current than R234. V=IR $I \propto \frac{1}{R}$

$$I_5 = 1.9 A - 0.543 A = 1.4 A$$

Therefore, the current through the 6-sl resistor is 1.4 A.

9)
$$R_1 = 4.0 \Omega$$
 :: $V_1 = I_1 R_1$
 $I_1 = 1.9 A$:: $V_1 = (1.9 A)(4.0 \Omega)$
 $V_1 = 7.6 V$

 $V_1 = I_1 K_1$ $V_2 = (1.9A)(4.0\Omega)$ The voltage drop across

the 4.0-\Omega resistor is 7.6 V.

G49.
$$R = \frac{Pl}{A}$$

$$R = \frac{Pl}{\pi R^2}$$

where l = length of wire and A = area of the cross-section and $\rho = resistivity$

$$\frac{\text{Wire 1}}{\pi r^2} \qquad \mathcal{R} = \frac{\rho L}{\pi r^2}$$

Wire 2 – radius 4R, length 16L Wire 3 - radius 5R, length L/3

Wire 4 - radius R/2, length 3L/2

wire 2
$$R = \frac{\rho(16L)}{\pi(4r)^2} = \frac{16(\rho L)}{16(\pi r^2)} = \frac{\rho L}{\pi r^2}$$

wire 3
$$R = \frac{\rho(\frac{L}{3})}{\pi(5r)^2} = \frac{\rho L}{3(25)(\pi r^2)} = \frac{1}{75} \cdot \frac{\rho L}{\pi r^2}$$

wire 4
$$R = \frac{P(\frac{3L}{2})}{\pi (\frac{r}{2})^2} = \frac{3(PL)}{2(\frac{1}{4})(\pi r^2)} = 6 \cdot \frac{PL}{\pi r^2}$$

:. Greatest R
$$\rightarrow$$
 Smallest Resistance
Wire 4 > Wires 1 and 2 > Wire 3

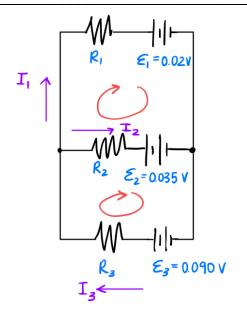
G51.
$$R_1 = R_2 = R_3 = 0.0025 \Omega$$

 $E_1 = 0.020 V$
 $E_2 = 0.035 V$
 $E_3 = 0.090 V$

Kirchhoff's Node Law:

$$I_3 - I_1 - I_2 = 0$$

 $I_3 = I_1 + I_2$



<u>kirchhoff'S loop law:</u>

Return to the Node law & Substitute

$$T_3 = T_1 + T_2$$

 $22V - T_2 = T_2 - 6V + T_2$
 $28V = 3I_2$
 $T_2 = 9.3A$

$$I_3 = 22 - 9.33 = \boxed{13 \text{ A}}$$

$$I_1 = 9.33 - 6 = \boxed{3.3 \text{ A}}$$

is 3.3 A and it moves from the positive terminal to the negative terminal.

G53.

$$\mathcal{E} \stackrel{+}{=} \qquad \qquad \begin{array}{c} R_1 = \\ 51 \text{ k}\Omega \end{array} \qquad \begin{array}{c} R_2 = \\ 19 \text{ k}\Omega \end{array}$$

$$R_3 = 27 \text{ k}\Omega$$

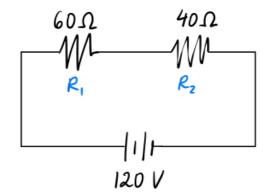
$$\begin{array}{lll}
\mathbb{O} & \mathcal{R}_{12} = \left(\frac{1}{\mathcal{R}_1} + \frac{1}{\mathcal{R}_2}\right)^{-1} \\
\mathcal{R}_{12} = \left(\frac{1}{51\kappa\Omega} + \frac{1}{19\kappa\Omega}\right)^{-1} \\
\mathcal{R}_{12} = 13.8 \, \kappa\Omega
\end{array}$$

②
$$Reg = R_{12} + R_3$$

 $Reg = 13.8 \times \Omega + 27 \times \Omega$
 $Reg = 41 \times \Omega$

: The equivalent resistance in the circuit is $41 \text{ k}\Omega$.

G55.

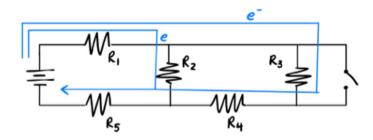


$$120V = V_1 + V_2$$

 $120V = IR_1 + IR_2$
 $120V = 60I + 40I$
 $120V = 100I$
 $I = 1.2 A$

:. The voltage across the 60-12 resistor is 72 V.

G57.



Paths electrons can take through the circuit with the switch open.

Calculation for Req

$$0 R_{34} = R_3 + R_4 = 2R$$

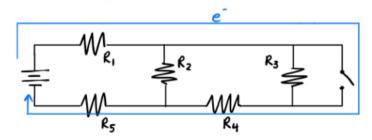
$$\frac{1}{R_{234}} = \frac{1}{R_2} + \frac{1}{R_{34}}$$

$$\frac{1}{R_{234}} = \frac{1}{R} + \frac{1}{2R}$$

$$R_{234} = \frac{2}{3}R$$

3 Req = R₁ + R₂₃₄ + R₅
Req = R +
$$\frac{2}{3}$$
R + R
Req = $\frac{8}{3}$ R

When the switch, there is a new path for electrons to flow through that has no resistance. Electrons like to follow the path of least resistance, therefore the paths involving resistors 2 and 3 will be effectively short-circuited (ie. no electrons will flow through them).



$$\frac{New \ Reg:}{Reg = R_1 + R_4 + R_5 = 3R}$$

$$3R > \frac{8}{3}R$$

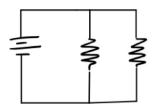
The overall resistance of the circuit increases when the switch is closed





Reg in series:

Must be greater than both R, and R2



Reg in parallel:

$$Req = \left(\frac{1}{R_1} + \frac{1}{R_2}\right)^{-1}$$

must be smaller than both R, and R2

 $\ddot{}$ The greater R is, the smaller I is.

- .. the bulbs will be brighter in the parallel circuit. More current will be drawn since resistance is smaller than if the bulbs were connected in series.
 - B) is correct.

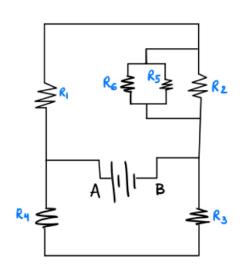
$$R = \frac{Pl}{A}$$

Resistance is directly proportional to the length of wire.

Therefore, if the length of wire increases by 0.5%, and assuming resistivity , and area of cross-section A remain unchanged, the resistance of the wire will likewise increase by 0.5%.

G63.
$$R_1 = R_2 = R_3 = R_4 = R_5 = R_6 = 100 \Omega$$

①
$$R_{56} = \left(\frac{100}{100} + \frac{100}{100}\right)^{-1} \Omega$$

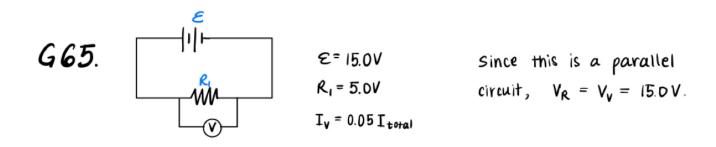


$$3 R_{1256} = 100 \Omega + 33.33 \Omega = 133.33 \Omega$$

$$\widehat{\mathfrak{D}} \, \mathcal{R}_{123456} = \mathcal{R}_{eq} = \left(\frac{1}{133.33} + \frac{1}{200} \right)^{-1} \, \mathcal{L}$$

$$\boxed{\mathcal{R}_{eq} = 80.0 \, \mathcal{L}}$$

Therefore, the equivalent resistance between terminals A and B is $80.0\,\Omega$.



Furthermore, recall that Ohm's law tells us that I
ot = R. Since electrons only have 2 possible paths to follow at the first junction in the circuit, the $5.0^{-}\Omega$ resistor must recieve 95% of the total current.

Since the 5.0- Ω resistor receives 19 times more current, it must have 19 times <u>less</u> resistance than the Voltmeter. Therefore, the voltmeter has a resistance of $19 \times 5.0 \Omega = 95 \Omega$.

To calculate the current through the EMF source:

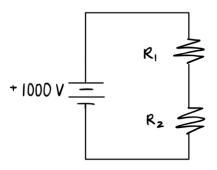
$$I_{V} = 0.05 I_{t} = \frac{V}{R}$$

$$I_{t} = 20 \left(\frac{15.0 V}{95 \Omega} \right)$$

$$I_{t} = 3.2 A$$

Therefore, the current passing through the EMF source is 3.2 A.

G67.



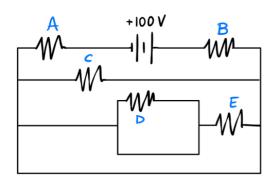
$$R_1 > R_2$$

$$I_1 = I_2$$

Power formula: P= I2R

- : Power is directly proportional to resistance and the current is the same for both resistors,
- resistor 1 will dissipate more power.

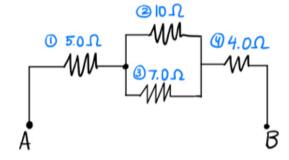
G69.



combinations of resistors in series:

A and B

G71.



1) Solving for Req

$$\frac{0}{R_{23}} = \frac{1}{10} + \frac{1}{7}$$

$$R_{23} = 4.12 \Omega$$

Therefore, the equivalent resistance between points A and B is 13Ω .

2) Solving for Current

①
$$T_t = \frac{V_{AB}}{R_{eq}} = \frac{100 \text{ V}}{13.12 \Omega} = \boxed{7.6 \text{ A}}$$

All current must go through resistors I and 4. This current is 7.6 A.

②
$$I \propto \frac{1}{R}$$
 $R_2 = 10\Omega$ $R_3 = \frac{7}{10}R_2$ $R_3 = 7\Omega$

$$I_3 = \frac{10}{7} I_2$$
 because V is constant.

$$I_{2} + I_{3} = I_{t}$$

$$I_{2} + \frac{10}{7} I_{2} = 7.6 A$$

$$\frac{17}{7} I_{2} = 7.6 A$$

$$I_{2} = 3.1 A$$

$$I_3 = \frac{10}{7}(3.1 A) = 4.5 A$$

The current through the $10-\Omega$ resistor is 3.1A. The current through the $7.0-\Omega$ resistor is $4.5\,A$.